

PHY-MAC Cross-Layer Cooperative Protocol Supporting Physical-Layer Network Coding

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Abstract

Cooperative communication has known as an effective solution to deal with the channel fading as well as to improve the network performances. Further, by combining the cooperative relaying technique with the physical-layer network coding (PNC), cooperative networks will obtain more benefits to improve the throughput and network resource utilization. In order to leverage these benefits, in this paper, we propose a PHY-MAC cross-layer cooperative protocol which can support PNC for multi-rate cooperative wireless networks with bidirectional traffic. The design objective of the proposed protocol is to increase the transmission reliability, throughput, and energy efficiency, as well as to reduce the transmission delay. Simulation results show that the proposed protocol outperforms the previous cooperative protocol as well as the traditional protocol in terms of network performance.

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1. Introduction

Nowadays, the increase in the number of people using mobile devices has leveraged the development of wireless networks. With the increased requirements in the quality of service for various applications, technical solutions need to be developed to improve the network performance such as the channel capacity, end-to-end throughput, transmission reliability, energy efficiency, and the network coverage. Cooperative transmission has been known as an effective method to exploit spatial diversity to enhance the quality of wireless channels at the physical layer. In the cooperative transmission multiple single-antenna devices can collaborate with one another to share their antennas with neighbouring partners in order to form a virtual multiple-input multiple-output (MIMO) system.

Recent development of data communication applications has shown that the traffic in

wireless networks is no longer unidirectional but mostly bidirectional. A typical example of bidirectional traffic is the peer-to-peer application such as voice and video communications. A challenging problem for the bidirectional traffic is how to design the data exchange protocol efficiently. In order to deal with this problem, cooperative relaying has been known as a promising technique in the wireless ad hoc networks [1]. In the more recent researches, cooperative relaying has also been proposed to combine with network coding (CC) to achieve more performance benefits, in particular, with the bidirectional traffic [2]–[5].

In wireless ad hoc networks, network coding can be implemented by two ways: (i) using the conventional network coding (CNC) in which the relay implements data decoding of received packets in two individual transmission time slots [6]; (ii) using the physical-layer network coding (PNC) in which the relay decodes data packets

received simultaneously from the two end nodes [7]. Compared with CNC, PNC has advantage in reducing the number of transmission phases and thus helps to increase the end-to-end throughput as well as to reduce the delay [8]–[10].

Most of recent researches on the bidirectional communication simply focused on combining PNC and the cooperative relaying [10]–[14]. In [10] Shiqiang et al. have proved that the PNC-based medium access control (MAC) protocol, namely PNC-MAC, has more advantages than the CNC-based MAC one in terms of the end-to-end throughput and delay. However, the drawback of this protocol is that it does not have a proper mechanism for reducing problems of hidden nodes in the network. Compared with the PNC-MAC protocol, the ANC-ARA protocol proposed in [14] has difference in that it does not need to know the queue status information of the neighboring nodes. Instead, it uses a special mechanism to avoid the problem of hidden nodes. The proposed cross-layer protocol in [15] uses PNC to support the bidirectional traffic efficiently. Compared with the protocols in [10] and [14], this protocol considers the protocol overheads as well as the contending time duration among optimal relay nodes in the design to increase the network performance. However, this PNC supported protocol still faces a problem of collisions during optimal relay selection. Clearly, a collision avoidance solution will help to increase further network performance in terms of end-to-end throughput or delay.

Motivated by the above problem, in this paper we propose an improved cross-layer cooperative MAC protocol which can support PNC and avoid the problem of collisions happened during the optimal relay selection process. The proposed protocol is designed to work in three modes: directional transmission, cooperative transmission for the unidirectional traffic, and cooperative relaying based on PNC for the bidirectional traffic. However, in this paper we will focus mainly on the last one. Compared with the protocols in [10]–[15], our proposed protocol has the following advantages:

- The physical-layer design of the protocol can be adapted to various cooperative diversity schemes depending on the channel conditions. In our protocol, more than one optimal relay node can be selected and partitioned in one or two relaying groups. Thanks to this arrangement, the process of cooperative relaying node selection can be implemented easily. Especially, in case there are two cooperative relaying groups, we can use the spatial diversity scheme based on the Alamouti distributed spatial-time block code (DSTBC) [16] to improve the transmission reliability.
- By letting the optimal relays in the same priority group send a signaling pulse of the same format the relay contending collision is avoided. As a result, the relay-contending time duration is reduced and the system throughput is thus improved.
- The MAC layer of the proposed protocol is designed to support two main functions: (i) adaptive relay selection mechanism supporting the bidirectional traffic; (ii) PNC is initiated by the cooperative relay nodes only if the bidirectional traffic is occurred. By this design, the proposed protocol can adapt itself flexibly to network environment variations to increase the end-to-end bidirectional throughput.

Our main contributions can be summarized as follows:

- A cooperative diversity transmission model based on optimal relay groups with the improved transmission reliability is proposed for cooperative wireless networks.
- The MAC layer protocol supporting PNC with the improved overall performance of network is introduced for multi-rate cooperative wireless networks.
- An analytical model of energy efficiency is introduced for the proposed protocol.

The remainder of the paper is organized as follows. Sect. 2 presents the network model under consideration. Sect. 3 describes the proposed protocol. The performance analysis of the proposed protocol is presented in Sect. 4. Simulation results are shown in Sect. 5. Finally, conclusions are drawn in Sect. 6.

2. System model

We consider a cooperative wireless network as illustrated in Fig. 1. The network consists of a source (S), a destination (D) placed apart at a distance of d , and a set of N intermediate nodes which are distributed randomly between S and D. All network nodes are equipped with only one single antenna and have limited transmitting power. The two end nodes are assumed to exchange data with each other in the bidirectional mode using the basic rate of $R_0 = 2\text{Mbps}$. Channels between each pair of nodes are assumed independent and affected by flat slow Rayleigh fading plus log-normal shadowing.

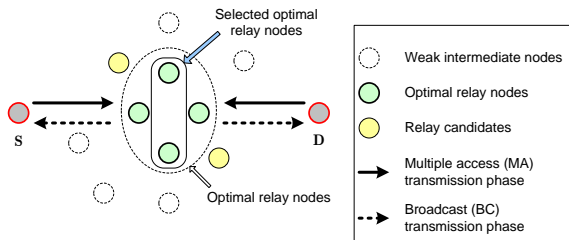


Fig. 1. Network model of the cooperative wireless network.

It is further assumed that among N intermediate nodes, only those capable nodes, referred to as relay candidates, will participate in the relay selection process. Those intermediate nodes with weak channel gain to S and D, referred to as weak intermediate nodes, will not participate into the relaying process. The optimal relay nodes are those relay candidates which have the same maximal cooperative rate. Moreover, the selected optimal relay nodes are the optimal relay nodes which are selected after the contention period. As shown in Fig. 1, several intermediate nodes can be selected as the optimal relays and the selected optimal relays.

3. Proposed PNC-supported PHY-MAC cross-layer cooperative protocol

3.1. Operations at the PHY layer

Assume that the PHY layer can support L different data rates r_1, r_2, \dots, r_L (for example, $L = 8$ in the IEEE 802.11a standard). Each network node uses a certain data rate if its estimated SNR is above a corresponding threshold $\gamma_l, \gamma_l \in (\gamma_1 < \gamma_2 < \dots < \gamma_L)$. Similar to the analysis of the cross-layer PHY-MAC protocol for unidirectional traffic in [17], we define the MAC cooperation region (CR) as a set of triple rates, $C := (R_1, R_{C_1}, R_{C_2}) \subseteq R^3$, such that the bidirectional effective payload transmission rate (EPTR) in relaying transmission is always larger than that in direct transmission. Here R_1, R_{C_1}, R_{C_2} denotes the direct rate, the first hop rate, and the second hop rate, relatively. In generally, the EPTR is given by $\frac{L_P}{T_O + T_P}$, with L_P, T_O, T_P being the payload length, the overhead time duration, and the payload time duration respectively. Hence, the condition for a relay to belong to the cooperation region is that the transmission delay for the cooperative bidirectional traffic is always less than that without cooperative relaying.

In order to improve the transmission reliability, we propose two cooperative relaying schemes which support bidirectional traffic. These schemes are shown in Fig. 2. In our proposed schemes, depending on the channel conditions each relaying group R_1 and R_2 can have one or more optimal relays selected by the MAC layer protocol.

3.1.1. Transmission based on one relaying group

In this case, the transmission scheme is illustrated in Fig. 2-a. In the scheme, bidirectional data exchange between S and D is performed over the multiple access (MA) phase and the broadcast (BC) phase. In the MA phase, the two end nodes S and D transmit simultaneously to R_1 . The signal received simultaneously at the i -th relay in the relaying group R_1 is given by

$$y_{R_1}^i = h_{SR_1}^i x_S + h_{DR_1}^i x_D + z_{R_1}^i, \quad (1)$$

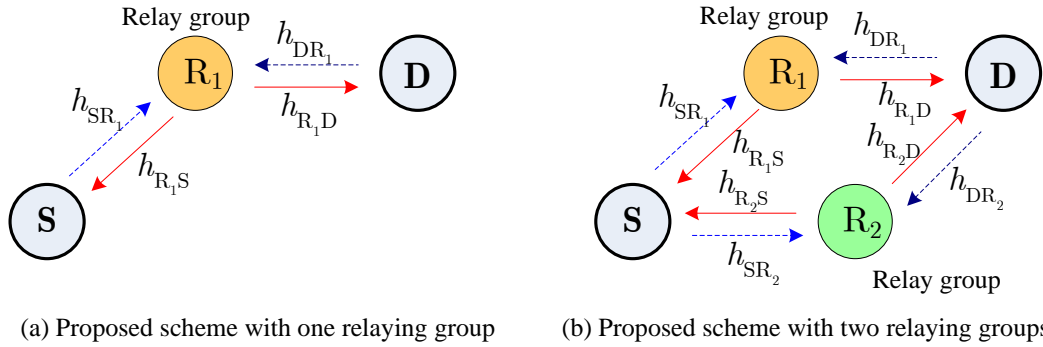


Fig. 2. Cooperative relaying model supporting bidirectional traffic.

where x_S and x_D are the transmitted signals from S and D, respectively. $h_{SR_1^i}$ and $h_{DR_1^i}$ are the fading coefficients of the channels from S and from D to the i -th relay of R_1 , respectively; $z_{R_1^i}$ is noise at the i -th relay of R_1 .

In the BC phase, the signals received at S and D are given respectively as follows:

$$y_S = \sum_{i=1}^{N_{R_1}} h_{R_1^i S} C_{\text{PNC}}(y_{R_1^i}) + z_i, \quad (2)$$

$$y_D = \sum_{i=1}^{N_{R_1}} h_{R_1^i D} C_{\text{PNC}}(y_{R_1^i}) + z_i, \quad (3)$$

where N_{R_1} is the number of relays of R_1 ; $C_{\text{PNC}}(\cdot)$ is a function of PNC. In this paper, we use the decoding and forwarding (DF) scheme at the relays and the PNC mapping function as in [7].

3.1.2. Transmission based on two relaying groups

The transmission for transmission scheme is drawn as Fig. 2-b. Assume that R_1 and R_2 consist of N_{R_1} and N_{R_2} optimal relays, where $N_{R_1}, N_{R_2} \geq 1$. In order to improve the transmission reliability of this scheme, we apply the Alamouti DSTBC scheme [16] to our considered transmission scheme. Similar to the case of one relaying group, the bidirectional data exchange between S and D also takes place over two phases (MA and BC). However, each phase uses two time slots for transmission. In two consecutive time slots of the MA phase, S and D send simultaneously their data vectors: $\mathbf{x}_S = [x_S^1, x_S^2]$ and $\mathbf{x}_D = [x_D^1, x_D^2]$, respectively to relays. The signals received at the

i -th relay of R_1 in two consecutive time slots are respectively given by

$$y_{R_1^i}^1 = h_{SR_1^i} x_S^1 + h_{DR_1^i} x_D^1 + z_i^1, \quad (4)$$

$$y_{R_1^i}^2 = h_{SR_1^i} x_S^2 + h_{DR_1^i} x_D^2 + z_i^2, \quad (5)$$

where, $h_{SR_1^i}$ and $h_{DR_1^i}$ are the Rayleigh fading coefficients of the link from S and D to the i -th relay of R_1 , respectively. z_i^1, z_i^2 are the noise occurred in each time-slot, respectively.

Similarly, the signals received at the j -th relay of R_2 during two consecutive time-slots of the MA phase are denoted by

$$y_{R_2^j}^1 = h_{SR_2^j} x_S^1 + h_{DR_2^j} x_D^1 + z_j^1, \quad (6)$$

$$y_{R_2^j}^2 = h_{SR_2^j} x_S^2 + h_{DR_2^j} x_D^2 + z_j^2. \quad (7)$$

In the BC phase, the selected optimal relays broadcast their PNC encoded signals to both S and D. Since the Alamouti DSTBC scheme is used, the signals received at S during two consecutive time slots are given by

$$y_S^1 = H_S^1 C_{\text{PNC}}(y_{R_1^i}^1) + H_S^2 C_{\text{PNC}}(y_{R_2^j}^2) + z_S^1, \quad (8)$$

$$y_S^2 = H_S^1 [-C_{\text{PNC}}(y_{R_1^i}^2)]^* + H_S^2 [C_{\text{PNC}}(y_{R_2^j}^1)]^* + z_S^2, \quad (9)$$

where

$$H_S^1 = \sum_{i=1}^{N_{R_1}} h_{R_1^i S} \quad \text{and} \quad H_S^2 = \sum_{j=1}^{N_{R_2}} h_{R_2^j S},$$

and the asterisk $*$ is used to denote the complex conjugation; z_S^1, z_S^2 are the noise occurred at the

source in each time slot, respectively. We also assume that the links between any two nodes in the network are reversible such that $h_{R_1^i S} = h_{SR_1^i}, h_{R_2^j S} = h_{SR_2^j}$.

Similar to the source, the signals received at the destination during two consecutive time slots of the BC phase are given by

$$y_D^1 = H_D^1 C_{PNC}(y_{R_1^i}^1) + H_D^2 C_{PNC}(y_{R_2^j}^2) + z_D^1, \quad (10)$$

$$y_D^2 = H_D^1 [-C_{PNC}(y_{R_1^i}^2)]^* + H_D^2 [C_{PNC}(y_{R_2^j}^1)]^* + z_D^2, \quad (11)$$

where

$$H_D^1 = \sum_{i=1}^{N_{R_1}} h_{R_1^i D} \quad \text{and} \quad H_D^2 = \sum_{j=1}^{N_{R_2}} h_{R_2^j D}, \quad (12)$$

z_D^1, z_D^2 are the noise at each time slot, respectively. Here, we also assume that $h_{R_1^i D} = h_{DR_1^i}, h_{R_2^j D} = h_{DR_2^j}$. Hence, based on the estimated channel status information (CSI), the source and destination can estimate the signals received from the optimal relays in two groups R_1 and R_2 , then decode \mathbf{x}_S and \mathbf{x}_D based on the XOR operation.

3.1.3. PNC for multirate adaptive modulation

In order to work in the multirate communication mode, network nodes need to use adaptive modulation. As a result, the PNC scheme needs to be realized appropriately for several modulation types. In this paper, we adopt the PNC modulation–demodulation mapping principle proposed in [7] for the adaptive modulation with set of transmission

rates according to the IEEE 802.11a standard [18]. The process of PNC mapping is illustrated in Fig. 3. In the figure, \oplus denotes the general binary operation for network-coding arithmetic. That is, applying \oplus on $m_i, m_j \in M_b$ gives $m_i \oplus m_j = m_k \in M_b$; M_b is a set of potential binary code-words depending on each modulation type. Assuming that the M_s -ary modulation is used, then M_s is a set of the potential modulation symbols. Let \square be the binary combination operation, then combination of $s_S, s_D \in M_s$ yields $s_S \square s_D = s_k \in M'_s$, where M'_s is the domain after the binary operation; each $s_k \in M'_s$ received by the relay node must be mapped to a demodulated symbol $m_k \in M_b$.

3.2. Operation at the MAC layer

The main goal of designing the MAC layer of the proposed protocol is to minimize the overhead time and the bidirectional payload transmission time while supporting the adaptive relay selection. The operation of the proposed MAC layer scheme is illustrated in Fig. 4.

The operation of the proposed MAC layer is described as follows

- **Source Initiation:** After a back-off interval, the source establishes the link to the destination node using the request-to-send (RTS) and clear-to-send (CTS) exchange handshake. In order to start, the source broadcasts the RTS frame to both the destination and intermediate nodes.
- **Destination Response:** If the destination receives the RTS frame correctly, it broadcasts the CTS frame to both the source and intermediate nodes after a SIFS (Short Inter-Frame Spacing) interval. In the case the destination also has its own data to send to the source, the information of the payload length L_{ds} is included into the CTS frames, if not the length L_{ds} is set to null.
- **Intermediate Node Processing:** When the intermediate node overhears the RTS and CTS frames exchanged between the source and the destination, it estimates the CSI

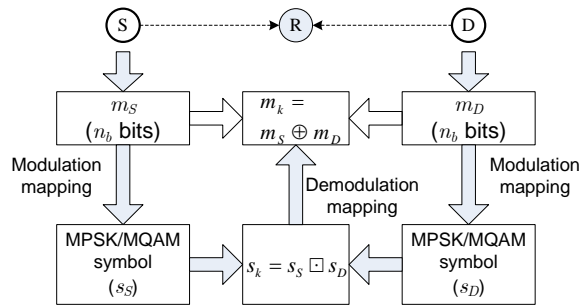


Fig. 3. The PNC mapping principle.

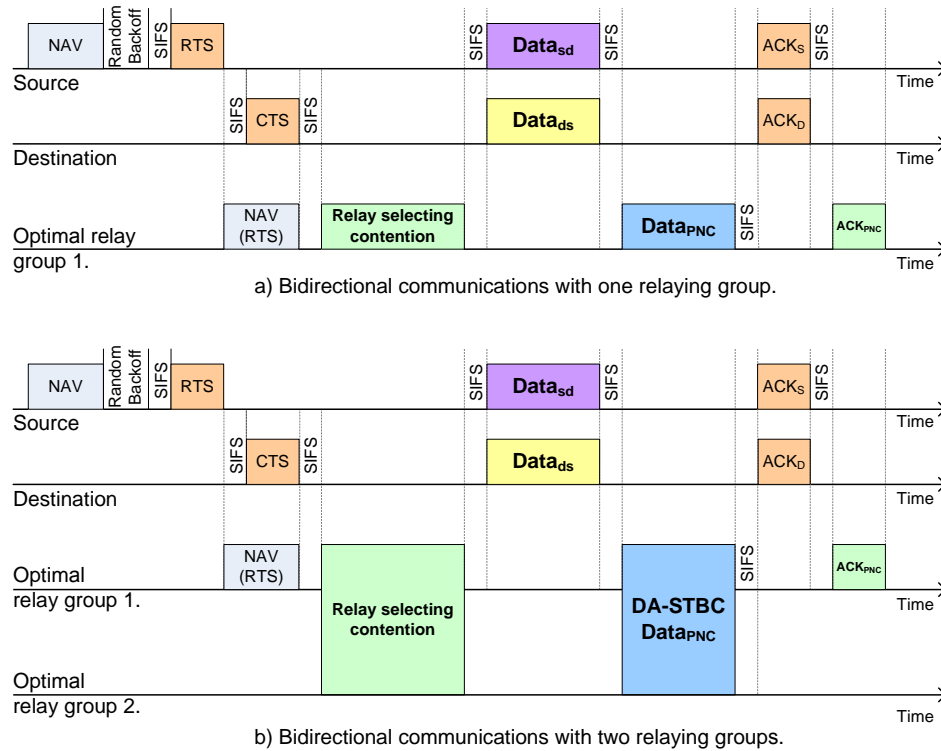


Fig. 4. The operation of the proposed MAC-layer protocol.

to determine its cooperative rate allocation in the cooperation region CR. If the intermediate node satisfies the condition of CR, it participates in the process of the optimal relay selecting contention.

- **Relay Transmission:** If a relay node is selected for the process of bidirectional cooperative communication, it uses transmission operations as in Fig. 2-a or Fig. 2-b. In contrast, it releases the relay contending process, and holds the waiting status.
- **Destination Acknowledgement:** After the source and destination have correctly received the data, they simultaneously send their ACK_S and ACK_D frames to the optimal relays after a SIFS interval. These relays then broadcast the ACK_{PNC} frame to both the source and destination.

3.3. Optimal relay selection

As mentioned in Section 3.1, in order to select the optimal relay using the distributed method, the optimal grouping algorithm works as follows. Given the direct transmission rate R_1 , there exist M potential cooperative rates R_h . A set of these cooperative rates are partitioned into G different priority groups, each consists of n_g relay members, where each member can be assigned to a different m priority level according to its identified data rate, so $M = \sum_{g=1}^G n_g$. Each relay candidate can determine its priority allocation in CR according to the g -th group-priority index and the m -th member-priority index. Based on these parameters, the MAC-layer protocol selects the optimal relay node through control and/or signaling messages. The process of optimal relay selecting contention is shown in Fig. 5 and is described as follows:

- Step 1: If a relay candidate finds its data rate allocation in CR, it decides to broadcast the

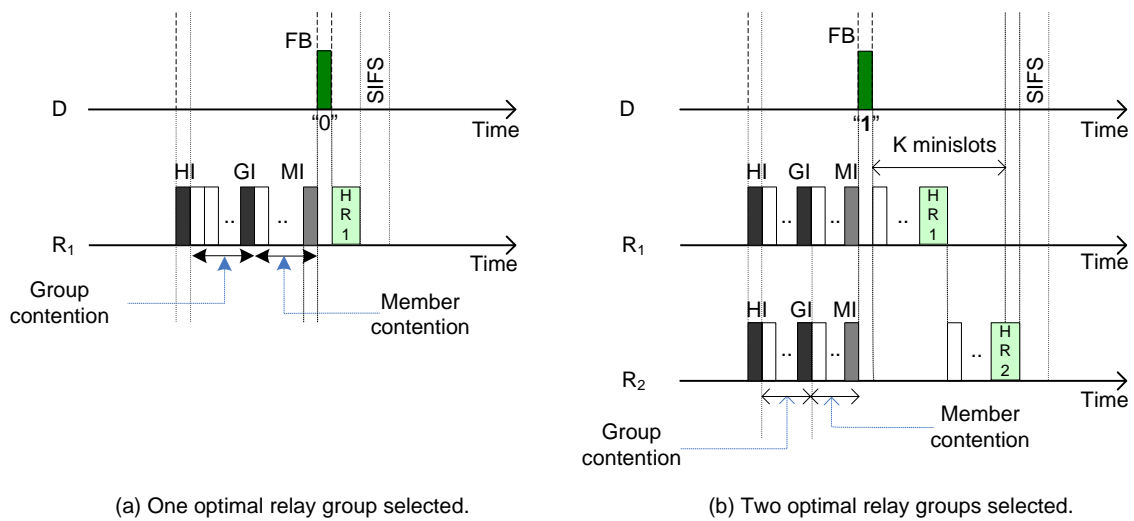


Fig. 5. Relay selection operation.

helper¹ indication (HI) signal to inform the source and destination its capability. If not it holds the silent status.

- Step 2: After the HI signal is sent, the relay candidate counts time down, starting from the g -th time-slot to 1, it then broadcasts the group indication (GI) signal to inform its group-priority allocation if overhears no GI signal.
- Step 3: Immediately after sending the GI signal, the relay candidate continues to count time down starting from the m -th time-slot to 1, it then broadcasts the helper member (MI) signal to inform its member-priority allocation if no MI signal was overheard. The relay candidates successfully sent the MI signal are called the optimal relays. After the MI signal is sent, the optimal relays wait for the feedback (FB) signal from the destination to determine the number of optimal relays occurred in the network. Without loss of generality, we assume that there exist n optimal relays and in order to estimate n we use the same method as in (25) of [5].

¹Note that in order to keep it consistent with the previous reference, we still use the term “helper” where necessary but its meaning is equivalent to “relay”.

- Step 4: The optimal relay compares the FB signal received with the “0” and “1” logic levels:

In case $FB = “0”$ (meaning that there exists only one optimal relay), it immediately broadcasts a help response pulse HR_1 to indicate the willingness to participate in the cooperative relaying process.

In case $FB = “1”$ (meaning that there exist more than one optimal relay), it randomly selects the k -th time-slot in K mini-slots to send the HR_1 signal if it overhears no HR_1 signal and remembers its allocation in the relaying group R_1 , or it sends the HR_2 signal if it overhears the HR_1 signal but no HR_2 signal and remembers its allocation in the relaying group R_2 .

The optimal relays successfully sent the HR_1 or HR_2 signal are the optimal relays selected for cooperative relaying data frames. Immediately after the HR_2 signal is sent, remaining optimal relays release the random contending process.

Note that in order to facilitate the distributed relay (helper) selection, the duration of all indication signals (i.e., the HI, GI, and MI signals) should be smaller than the backoff slot time.

4. Performance analysis

4.1. Transmission latency

Concentrating on the bidirectional communication mode, we estimate the time duration for two data packets of two end nodes (the source and the destination) exchanged under the proposed protocol. The overall time for bidirectional transmissions, starting at the initial time of the source until both the source and destination nodes receiving their expected data frames correctly, is determined by

$$E[T_{\text{total}}] = E[T_d] + E[T_{\text{Coop}}], \quad (13)$$

where, $E[T_d]$ is the average time duration for direct transmissions when there exists no cooperative relay; $E[T_{\text{Coop}}]$ is the average time duration for bidirectional cooperative transmissions. Because $E[T_d]$ can be calculated easily depending on the network configuration, in this paper we concentrate on deriving the $E[T_{\text{Coop}}]$ formula.

To estimate $E[T_{\text{Coop}}]$, we assume that there exists at least one optimal relay node participating in the bidirectional cooperative relaying process. Firstly, we know that the frame transmission time depends on the frame error probability, which in turn relates to the bit error probability (BEP). Therefore, we denote $P_{e,sd}$ the BEP on the channel between the source and the destination, and $P_{fe_1}, P_{fe_2}, P_{fe_3}, P_{fe_4}$ the event probabilities that the error occurs in the frames RTS, CTS, DATA and ACK, respectively. These probabilities are given as follows

$$P_{fe_1} = 1 - (1 - P_{e,sd})^{L_{\text{RTS}}}, \quad (14)$$

$$P_{fe_2} = (1 - P_{e,sd})^{L_{\text{RTS}}}(1 - (1 - P_{e,sd})^{L_{\text{CTS}}}), \quad (15)$$

$$P_{fe_3} = (1 - P_{e,sd})^{L_{\text{RTS}}+L_{\text{CTS}}}\bar{P}_{\text{DATA}}, \quad (16)$$

$$P_{fe_4} = (1 - P_{e,sd})^{L_{\text{RTS}}+L_{\text{CTS}}}(1 - \bar{P}_{\text{DATA}})\bar{P}_{\text{ACK}}, \quad (17)$$

where L_{RTS} and L_{CTS} is the length of the frames RTS, CTS respectively; $\bar{P}_{\text{DATA}}, \bar{P}_{\text{ACK}}$ are the average transmission error probabilities of the frames DATA and ACK.

Let $\bar{P}_{(\text{DATA}, \text{E2E})}$ be the end-to-end BEP at the end nodes (the source and the destination). Then, we obtain

$$\bar{P}_{\text{DATA}} = 1 - \left(1 - \bar{P}_{(\text{DATA}, \text{E2E})}\right)^{2L_{\text{DATA}}},$$

with L_{DATA} denoting the data frame length sent by the source and the destination.

Because the transmission scheme of the frames ACK and DATA is the same, we also can obtain the transmission error probability of the frame ACK as $\bar{P}_{\text{ACK}} = 1 - \left(1 - \bar{P}_{(\text{ACK}, \text{E2E})}\right)^{2L_{\text{ACK}}}$, where L_{ACK} is the ACK length sent by the source and the destination, and $\bar{P}_{(\text{ACK}, \text{E2E})}$ is the end-to-end average BEP that a bit in the ACK frame is not received correctly at the end nodes.

Hence, the transmission error probability in the case of the bidirectional cooperative relaying is $P_e^c = \sum_{i=1}^4 P_{fe_i}$, and the successful transmission probability for the case of the bidirectional cooperative relaying is $P_s^c = (1 - P_e^c)$. The time duration for the above probability events is given by

$$T_{fe_1} = T_{\text{RTS}} + T_{\text{CTS}} + 2T_{\text{SIFS}} + 2t_{\text{prop}}, \quad (18)$$

$$T_{fe_2} = T_{\text{RTS}} + T_{\text{CTS}} + 2T_{\text{SIFS}} + 2t_{\text{prop}}, \quad (19)$$

$$T_{fe_3} = T_{fe_2} + T_{\text{cont}} + T_{\text{DATA}} + T_{\text{ACK}}, \quad (20)$$

$$T_{fe_4} = T_{fe_3}, \quad (21)$$

where a frame is considered successfully transmitted only when it and all its previous frames were also successfully transmitted. $T_{\text{RTS}}, T_{\text{CTS}}$, and t_{prop} is the time duration of the frames RTS, CTS and the propagation time, respectively. $T_{\text{DATA}}, T_{\text{ACK}}$ are the time duration for the bidirectional data transmission and the bidirectional transmission of frames ACK; T_{SIFS} is the SIFS time duration; T_{cont} is the time duration for the relay selecting contention, and is calculated by

$$T_{\text{cont}} = T_{\text{HI}} + (g - 1)t_{\text{slot}} + T_{\text{GI}} \\ + (m - 1)t_{\text{slot}} + T_{\text{MI}} + T_{\text{FB}} + E[T(n, k)], \quad (22)$$

where $T_{\text{HI}}, T_{\text{GI}}, T_{\text{MI}}$, and T_{FB} are the time duration of the signals HI, GI, MI, and FB respectively; t_{slot} is the mini-slot time interval.

$E[T(n, k)]$ denotes the average time duration for the random contending process to send the signals HR₁ and HR₂, and is calculated as follows

$$E[T(n, k)] = \begin{cases} T_{HR_1} + T_{SIFS}, & \text{if } n = 1; \\ P_1 \sum_{k=1}^K [(k-1)t_{slot} + T_{HR_1} + (K-k)t_{slot} + T_{SIFS}] \\ + P_2 \sum_{k=1}^{K-1} \sum_{v=k+1}^K [(k-1)t_{slot} + T_{HR_1} \\ + (v-k-1)t_{slot} + T_{HR_2} + T_{SIFS}], & \text{if } n \geq 2 \end{cases} \quad (23)$$

where P_1 is the probability that all n optimal relays select the same k -th time slot in K mini-slots, and P_2 is the probability that more than one of n the optimal relays select two different k -th time-slots in K mini-slots. Given K and $n \geq 2$, these probabilities are determined by $P_1 = \left(\frac{1}{K}\right)^n$, and so $P_2 = 1 - P_1$.

Through the above analysis, the average time duration for retransmission in the case of the bidirectional cooperative relaying is obtained as follows

$$E[T_e^c] = \sum_{i=1}^4 P_{fe_i} T_{fe_i}. \quad (24)$$

Therefore, the overall average time duration is determined by

$$E[T_{Coop}] = P_s^c (E[T_P] + E[T_O]) + E[T_e^c], \quad (25)$$

where $E[T_P]$ is the bidirectional payload transmission time, $E[T_P] = E\left[\frac{2W}{\min(R_{C_1}, R_{C_2})}\right]$, and R_{C_1} and R_{C_2} are the transmission rates from the source and destination to the optimal relaying groups, respectively. $E[T_O]$ is the overhead time, $E[T_O] = T_h + T_{cont} + 2T_{DO} + 2T_{SIFS} + T_{ACK}$. Here T_h is the time duration for the handshake process, and is determined by $T_h = T_{RTS} + T_{CTS} + 2T_{SIFS} + 2t_{prop}$; T_{DO} is the data overhead time. T_{ACK} is the time duration for the frames ACK, and $T_{ACK} = \frac{2L_{ACK}}{R_o} + 2T_{SIFS} + 2t_{prop}$.

4.2. The throughput formula

The cooperative throughput of the system can be defined as the average payload account transmitted successfully at the bidirectional

relaying mode per the overall time, and is calculated as follows

$$Q_{Coop} = \frac{E[\text{Payload}]}{E[T_{Coop}]} = \frac{P_s^c(2W)}{P_s^c(E[T_P] + E[T_O]) + E[T_e^c]}, \quad (26)$$

where W is the payload length of the end nodes (the source and the destination). In this paper, to simplify the analysis we assume that both the source and the destination have the same payload length.

4.3. Analytical model for energy efficiency

The average consumed energy for the bidirectional communication is determined by the average consumed energy for the successful cooperative relaying $E[\varepsilon_s]$ plus the average consumed energy for the number of re-transmission $E[\varepsilon_r]$:

$$E[\varepsilon_{Coop}] = E[\varepsilon_s] + E[\varepsilon_r]. \quad (27)$$

In order to clarify the above equation, we try to compute each term analytically. We consider three different modes: (i) the transmission mode: when the node is transmitting data/control packets; (ii) reception mode: when the node is receiving data/control packets; (iii) idle mode: when the node is sensing the medium without performing any action. The power levels associated to each mode are P_T, P_R, P_I , respectively. Furthermore, the relationship between energy and power is given by $\varepsilon = P \cdot t$, where the terms ε, P, t represent the energy, the power and the time, respectively.

With the network model under consideration presented in Section 2, the average energy consumption for the successful transmission is determined as follows

$$E[\varepsilon_s] = E[\varepsilon_h] + E[\varepsilon_{cont}] + E[\varepsilon_D] + E[\varepsilon_{ACK}], \quad (28)$$

where the energy $E[\varepsilon_h]$ consumed for the handshake process is:

$$E[\varepsilon_h] = [P_T + (N+1)P_R]T_{RTS} + (N+2)P_I T_{SIFS} + [P_T + (N+1)P_R]T_{CTS} + (N+2)P_I T_{SIFS}. \quad (29)$$

$$\begin{aligned}
& E[\varepsilon_{\text{cont}}] \\
& = (M_c P_T + 2P_R + (N - M_c + 2)P_I)T_{\text{HI}} + (N + 2)P_I(g - 1)t_{\text{slot}} + (n_g P_T + (M_c - n_g + 2)P_R + (N - M_c)P_I)T_{\text{GI}} \\
& + (N + 2)P_I(m - 1)t_{\text{slot}} + (n P_T + (n_g - n + 2)P_R + (N - n_g)P_I)T_{\text{MI}} + (P_T + (n + 1)P_R + (N - n)P_I)T_{\text{FB}} \\
& + F_{(n=1)} \left\{ (P_T + 2P_R + (N - 1)P_I)T_{\text{HR}_1} + (N + 2)P_I T_{\text{SIFS}} \right\} + F_{(n \geq 2)} \left\{ P_1 \sum_{k=1}^K [(N + 2)P_I(k - 1)t_{\text{slot}} \right. \\
& + (N_{R_1} P_T + 2P_R + (N - N_{R_1})P_I)T_{\text{HR}_1} + (N + 2)P_I((K - k)t_{\text{slot}} + T_{\text{SIFS}})] \\
& + P_2 \sum_{k=1}^{K-1} \sum_{v=k+1}^K [(N + 2)P_I(k - 1)t_{\text{slot}} + (N_{R_1} P_T + (n - N_{R_1} + 2)P_R + (N - n)P_I)T_{\text{HR}_1} \\
& \left. + (N + 2)P_I(v - k - 1)t_{\text{slot}} + (N_{R_2} P_T + (n - N_{R_2} + 2)P_R + (N - n)P_I)T_{\text{HR}_2} + (N + 2)P_I T_{\text{SIFS}} \right\}, \tag{30}
\end{aligned}$$

$E[\varepsilon_{\text{cont}}]$ consumed for the process of the optimal relay contention is calculated by (30). Note that M_c is a set of cooperative relay candidates. $F_{(n=1)}$ and $F_{(n \geq 2)}$ are the logic functions, which return value 1 if the condition of n is satisfied, otherwise 0, N_{R_1} and N_{R_2} is the number of optimal relay members belonging to the group R_1 and R_2 , respectively.

The energy consumption of the data transmission process is calculated as:

$$\begin{aligned}
E[\varepsilon_{\text{D}}] & = [2P_T + (N_{R_1} + N_{R_2})P_R \\
& + (N - N_{R_1} - N_{R_2})P_I]T_{\text{DATA}} \\
& + (N + 2)P_I T_{\text{SIFS}} + [(N_{R_1} + N_{R_2})P_T + 2P_R \\
& + (N - N_{R_1} - N_{R_2})P_I]T_{\text{DATA}} + (N + 2)P_I T_{\text{SIFS}}. \tag{31}
\end{aligned}$$

The ACK frame transmission process consumes the energy

$$\begin{aligned}
E[\varepsilon_{\text{ACK}}] & = [2P_T + (N_{R_1} + N_{R_2})P_R \\
& + (N - N_{R_1} - N_{R_2})P_I]T_{\text{ACK}} \\
& + (N + 2)P_I T_{\text{SIFS}} + [(N_{R_1} + N_{R_2})P_T + 2P_R \\
& + (N - N_{R_1} - N_{R_2})P_I]T_{\text{ACK}} + (N + 2)P_I T_{\text{SIFS}}. \tag{32}
\end{aligned}$$

In order to estimate the energy consumption for the retransmission $E[\varepsilon_r]$, the analysis is based

on the event probabilities occurred in equation (14)–(17), and the time duration in equation (18)–(21). Let E_1, E_2, E_3 and E_4 be the average energy consumption according to the frame error events. We can calculate these terms as follows

$$\begin{aligned}
E_1 & = [P_T + (N + 1)P_R]T_{\text{RTS}} \\
& + (N + 2)P_I(T_{\text{SIFS}} + T_{\text{CTS}}); \\
E_2 & = [P_T + (N + 1)P_R]T_{\text{RTS}} + (N + 2)P_I T_{\text{SIFS}} \\
& + [P_T + (N + 1)P_R]T_{\text{CTS}} + (N + 2)P_I T_{\text{SIFS}}; \\
E_3 & = E_h + E[\varepsilon_{\text{cont}}] + E[\varepsilon_{\text{D}}] + (N + 2)P_I T_{\text{ACK}}; \\
E_4 & = E_h + E[\varepsilon_{\text{cont}}] + E[\varepsilon_{\text{D}}] + E[\varepsilon_{\text{ACK}}]. \tag{33}
\end{aligned}$$

Hence, $E[\varepsilon_r]$ is determined by:

$$E[\varepsilon_r] = \sum_{i=1}^4 P_{f_{e_i}} E_i. \tag{34}$$

The energy efficiency, measured in [bits/Joule], can be defined as the amount of delivered useful data per energy unit. Considering the proposed protocol operation, the energy efficiency η for the bidirectional communication mode can be written as follows

$$E[\eta] = \frac{E[\text{Payload}]}{E[\varepsilon_{\text{Coop}}]} = \frac{P_s^c(2W)}{E[\varepsilon_s] + E[\varepsilon_r]}. \tag{35}$$

5. Simulation results

In order to evaluate the performance of the proposed protocol, we implement the Monte Carlo simulation for some scenarios. Further, all simulations are set up for the bidirectional traffic.

5.1. BER performance

In order to obtain the BER performance the two schemes in Fig. 2-a and Fig. 2-b are employed for simulation. In these schemes R_1 consists of N_{R_1} optimal relay nodes, and R_2 consists of N_{R_2} optimal relay nodes. The link between each node pair are assumed to be independent and affected by slowly varying flat Rayleigh fading. Noise power is set to unity, i.e., $N_0 = 1$. In case of the scheme in Fig. 2-a, we set the power of the source P_s , the destination P_d , and the relay P_r equal, i.e. $P_s = P_d = P_r = P$. In case of the scheme in Fig. 2-b, $P_s = P_d = P$ and $P_r = P/2$. BER performance is evaluated versus P/N_0 . For simplicity, we use the BPSK modulation for all the schemes. Simulation results are shown in Fig. 6.

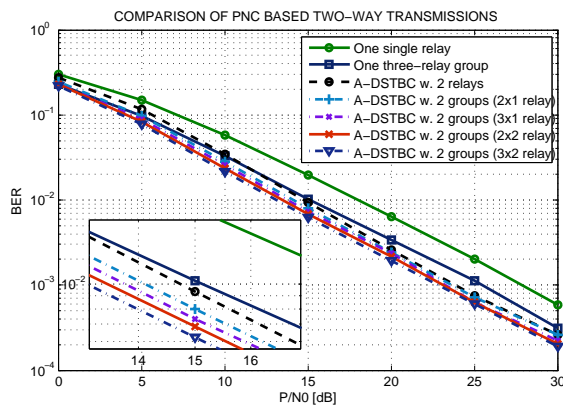


Fig. 6. BER performance comparison of different schemes.

We can observe clearly from Fig. 6 that the performance of the schemes with two relay groups is better than that with one relay group. It can be explained using the fact that the schemes with two relay groups employ the Alamouti DSTBC with the maximal ratio combining (MRC) reception, so they can achieve more power gain to improve transmission reliability. Furthermore, the performance of the scheme with

one relay group is improved when the number of optimal relay members of the group increases. This is because the destination receives more power from different relaying paths, so the SNR value is increased leading to the reduced BER.

5.2. Throughput and delay evaluation

In order to evaluate the throughput and delay through simulation, we use the system model in Fig. 1 with $N = 40$ immediate nodes between the source and the destination. The links between each node pair are assumed to be independent and affected by slowly varying flat Rayleigh fading with the log-normal shadowing effects, and the path loss with the loss coefficient 3,5. The transmission power is set to 1 W. The payload length is $W = 1500$ Bytes. In addition, the adaptive modulation scheme employs either BPSK, 4-QAM, 16-QAM, or 64-QAM depending on the channel quality. This is equivalent to the instantaneous SNR thresholds of 6, 15, 21, and 27 dB, respectively. In order to evaluate the throughput and delay, it is required that BEP needs to be estimated. This can be done based on the average SNR of the transmission links. With the two-phase data transmission scheme, under the assumption that the CSI is perfectly known, the end-to-end average BEP can be estimated from the average BEP of the first hop transmission (MA phase) and the second hop transmission (BC phase). However, to simplify the simulation, we assume that $P_{(DATA, E2E)}$ is given. The MAC and PHY parameters are based on the IEEE 802.11a standard. To reveal the advantage of the proposed protocol, we compare its performance with the previous cooperative MAC [15] and the traditional MAC protocol 802.11 DCF following the distance between the source and the destination or the network radius. In order to obtain the performance results over different network radii, we set up a simulation scenario in which the network radius is varying while the number of nodes is fixed. As the network radius increases, the distance between network nodes tends to increase leading to different received SNR due to log-normal shadowing fading [19] at each node. According

to 8 transmission rates (6, 9, 12, 18, 24, 36, 48, and 54 Mbps) we choose 8 corresponding SNR thresholds (6, 12, 15, 18, 21, 24, 27, and 30 dB). Depending on the received SNR, the cooperative transmission rates R_{C_1} and R_{C_2} from S and D to each intermediate node take one of the 8 given rates. As the resulted cooperative rates relate with T_P , T_O and T_e^c , the transmission delay can be obtained with the varying network radius via (25), while given W the cooperative throughput Q_{Coop} can be obtained via (26). Similarly, the energy efficiency can be obtained via ε_s and ε_r , which in turn depend on ε_D via (28), (33) and (34), and thus on T_{DATA} via (31). As T_{DATA} is decided by the two given cooperative rates, we can obtain the energy efficiency versus the network radius accordingly.

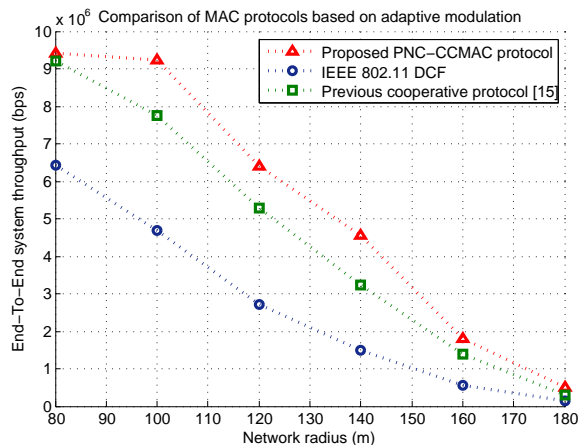


Fig. 7. Throughput performance.

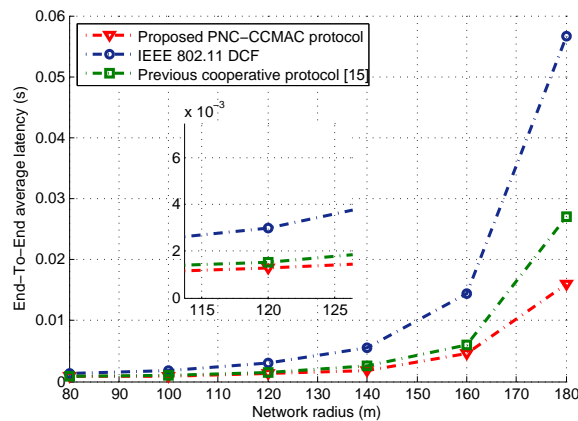


Fig. 8. Delay performance.

Simulation results for the throughput and delay performance are shown in Fig. 7 and Fig. 8, respectively. Observing Fig. 7 we can see that the throughput of all three protocols decreases rapidly when the network radius increases. This is because when the network radius increases the distance between network nodes also increases, leading to the drop in channel quality as well as the data transmission rates and thus the end-to-end throughput. To be more detailed, because the term $E[T_P]$ in (26) is the inverse function of the data transmission rates as analyzed in 4.1, when these rates decrease the term $E[T_P]$ will increase and the throughput decreases. However, the proposed protocol still achieves the best throughput performance, followed by the previous cooperative MAC protocol [15], and finally, the traditional protocol 802.11 DCF. It is interestingly noted that at the radius range from 80 m to 100 m, the throughput of the proposed scheme decreases more slowly compared to other ones. This can be explained by using the fact that our scheme uses adaptive modulation. Within this certain network radius, the channel quality is good and thus high modulation level is used leading to higher throughput. As the radius increases due to increase in the path loss and transmission error, lower modulation level is required and thus the throughput decreases more rapidly.

Fig. 8 shows that the end-to-end latency of the three above mentioned protocols increases with the network radius. This is because the throughput decreases with the network radius as explained above leading to increase in the transmission time and also the end-to-end latency. However, it can be clearly seen that our proposed protocol exhibits better delay performance than other protocols. This is due to the fact that the proposed protocol uses the short signaling pulses (HR_1 and HR_2) instead of the forward-to-send (FTS) control frame in the previous cooperative protocol [15]. To be more specific, the length of FTS is equal to that of the CTS frame (304 bits in the IEEE 802.11a standard) and equivalent to about 17 time slots while the length of HR_1 and HR_2 is just equivalent to

two time slots. This causes $E[T_O]$ in equation (25) to be neglected. In addition, by using these signaling pulses, the receiver does not need to decode each bit correctly. As a result, the retransmission time $E[T_C^c]$ in equation (25) is also reduced. Therefore, $E[T_{Coop}]$ in equation (25) decreases for the proposed protocol. Moreover, the proposed protocol uses a more effective relay contention mechanism as well as adaptive relay selection leading to significant reduction in the protocol overhead.

5.3. Energy efficient performance

To evaluate the energy efficiency of the proposed protocol we use the same simulation model in Section 5.2. However, the transmission power is now set to $P_T = 1.000$ mW, and the received and idle power is $P_R = P_I = 700$ mW. The simulation results are shown in Fig. 9.

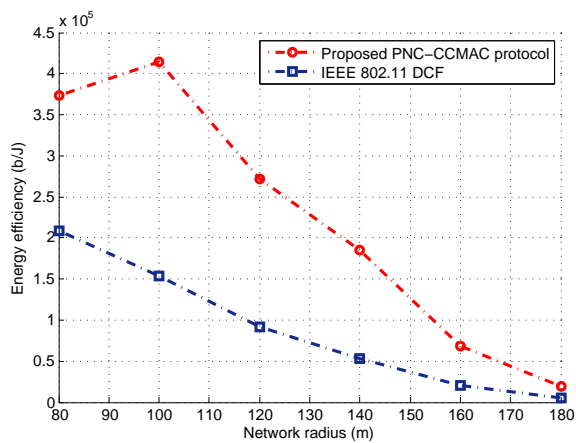


Fig. 9. Energy efficient performance.

We can see from Fig. 9 that the energy efficiency of the protocols decreases gradually when the network radius increases. This is because BER increases when the network radius increases, leading to the increase in the number of re-transmissions. As a result the operating time of the network nodes is increased or the energy consumption for the re-transmission $E[\varepsilon_r]$ in equation (35) is increased, leading to the decreased energy efficiency. However, the proposed protocol always achieves better energy efficiency than the IEEE 802.11 DCF over all network radius. Noted interestingly at the

network radius of 100 m that the energy efficiency is even higher than at 80 m. The reason is that the scheme(1,0) occurs more frequently than the others and with this scheme there will be no random contention². This means that only one optimal relay is selected to send the HR₁ signal right after the MI signal a T_{FB} interval. The data transmission phase is then activated and thus energy consumption is reduced for this scheme. As a result, the average consumed energy at the network radius 100 m is reduced, and thus the energy efficiency is higher.

Further, Fig. 10 illustrates the dependence of transmission scheme distribution on the network radius as well as the network configuration. The transmission scheme can be varied upon the channel conditions according to the network radius. Using simulation we can show that the scheme with two separated relays, scheme(1,1), occurs more frequently, followed by the one with one relay, scheme(1,0), and then the one with two relay groups, scheme(1,2). These three schemes can support bidirectional communication with higher power gain while the energy consumption is lower because the number of selected optimal relay members are not many compared with the number optimal relays occurred in the network. The remaining schemes with larger a and/or b occur at very low density. This observation also confirms the effectiveness of the relay selection method.

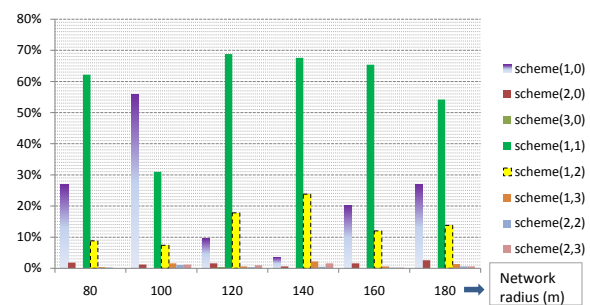


Fig. 10. Distribution of transmission schemes.

²We use the notation “scheme(a,b)” to denote each type of the transmission schemes presented in Fig. 2, where a is the number of the optimal relays in the relay group R_1 , and b is the number of the optimal relays in the relay group R_2

6. Conclusions

In this paper, we have proposed a PHY-MAC cross-layer cooperative protocol which can support PNC for cooperative wireless networks with bidirectional traffic. The proposed cross-layer protocol considers both the MAC layer and the PHY layer operation. We have shown by simulation that the proposed protocol can work flexibly in realistic channel conditions and achieve better performance than the previous protocol as well as the traditional protocol in terms of the system throughput, end-to-end latency, and the energy efficiency. With the above advantages, the proposed protocol can be employed in various ad hoc cooperative wireless networks.

Appendix A. Derivation of $E[T(n, k)]$ [B.1]

Based on the relay selection operation in Fig. 5, we can calculate $E[T(n, k)]$ for the following two cases:

Case 1: $n = 1$

Since there is only one optimal relay, it sends HR_1 to inform S and D its willingness to participate in the cooperative transmission process. After an SIFS interval, the data transmission process is initiated. Hence, $E[T(n, k)]$ is given by

$$E[T(n, k)] = T_{HR_1} + T_{SIFS}. \quad (A.1)$$

Case 2: $n \geq 2$

In this case, since more than one optimal relay participate in the random contending process, there are two possibilities: (i) All optimal relays select the same k -th time-slot in the K mini-slots. These optimal relays broadcast the HR_1 signal at the k -th time slot. In the remaining $(K - k)$ time slots, the network nodes stay at the waiting state. After an SIFS interval, the data transmission process is initiated. Let P_1 be the probability that all n optimal relays select the same k -th time slot

in K mini-slots. Then, $E[T(n, k)]$ is calculated as

$$E[T(n, k)] = P_1 \sum_{k=1}^K \left[(k-1)t_{\text{slot}} + T_{HR_1} + (K-k)t_{\text{slot}} + T_{SIFS} \right]. \quad (A.2)$$

(ii) Two optimal relay groups select two different time slots k and ν , respectively. The first optimal relay group sends the HR_1 signal after $(k-1)$ time slots and the second optimal relay group sends the HR_2 signal after $(\nu - k - 1)$ time slots. After an SIFS interval, the data transmission process is initiated. Let P_2 be the probability that more than one of n the optimal relays select two different time slots (the first group selects the k -th time-slot and the second selects the ν -th time-slot) in K mini-slots. Then, $E[T(n, k)]$ is calculated as

$$E[T(n, k)] = P_2 \sum_{k=1}^K \sum_{\nu=k+1}^K \left[(k-1)t_{\text{slot}} + T_{HR_1} + (\nu - k - 1)t_{\text{slot}} + T_{HR_2} + T_{SIFS} \right]. \quad (A.3)$$

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